An Acceleration Processor for Data Intensive Scientific Computing

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SUMMARY Scientific computations for diffusion equations and ANNs (Artificial Neural Networks) are data intensive tasks accompanied by heavy memory access; on the other hand, their computational complexities are relatively low. Thus, this type of tasks naturally maps onto SIMD (Single Instruction Multiple Data stream) parallel processing with distributed memory. This paper proposes a high performance acceleration processor of which architecture is optimized for scientific computing using diffusion equations and ANNs. The proposed architecture includes a customized instruction set and specific hardware resources which consist of a control unit (CU), 16 processing units (PUs), and a non-linear function unit (NFU) on chip. They are effectively connected with dedicated ring and global bus structure.Each PU is equipped with an address modifier (AM) and 16-bit 1.5 k-word local memory (LM). The proposed processor can be easily expanded by multi-chip expansion mode to accommodate to a large scale parallel computation. The prototype chip is implemented with FPGA. The total gate count is about 1 million with 530, 432-bit embedded memory cells and it operates at 15 MHz. The functionality and performance of the proposed processor is verified with simulation of oil reservoir problem using diffusion equations and character recognition application using ANNs. The execution times of two applications are compared with software realizations on 1.7 GHz Pentium IV personal computer. Though the proposed processor architecture and the instruction set are optimized for diffusion equations and ANNs, it provides flexibility to program for many other scientific computation algorithms.

key words: SIMD, FPGA, artificial neural networks, diffusion equations, image processing

1. Introduction

The scientific computations have demanded high performance computing power and have a great potential for SIMD parallel processing. SIMD architectures have been adopted effectively on the applications of image processing, matrix operations, partial differential equations, artificial neural networks, multimedia processing, etc.

Previously, SIMD architecture was realized in the form of massively parallel computer system starting from the first SIMD machine project, ILLIAC IV\cite{1}. They usually consisted of high performance host computer and data parallel unit including few hundreds or thousands of simple processing elements, memory system, and a global array control unit\cite{2}–\cite{4}. These SIMD machines were very large, complex, and expensive parallel supercomputers.

As the VLSI technology growing, architecturally new SIMD array processors, in which the processor and memory were integrated into a single chip to overcome the memory access bottleneck, were introduced in the form of special purpose processor or coprocessor and intelligent memory systems of a workstation or server\cite{5}–\cite{8}. The majority of these have the same concept to connect many simple processors together for fast parallel processing, and they are dedicated to a specific application in the lack of generalities. This application specific hardware limits the range of applications and causes the developed processor price high.

Recently, the aids of growing fabrication technology and CAD tool advance, which allow the implementation of a complex system on a chip in relatively low cost, have brought the advent of the parallel system based on DSP array processors and the parallel processor implementation optimized for scientific computing and neural networks. The former offers high flexibility, however, the computational efficiency is not high enough for certain applications\cite{9}–\cite{11}. The later approach implements PUs with relatively low performance arithmetic unit and local memory for each PU\cite{12}–\cite{15}. The memory access bottleneck is overcome by distributed memory and the computing power is obtained by parallelism. The main drawbacks of the parallel implementation are low computational efficiency in certain application and lower flexibility when it is compared with the former approach.

To overcome the limits of the previous SIMD processors, this paper proposes a flexible SIMD processor with distributed memory taking full advantage of the application specific instruction set and hardware resources; AM, NFU, ring and global buses, and multi-chip expansion. These features are optimally customized for achieving high computational efficiency in data intensive applications while providing flexibility. For example, the applications using diffusion equations and ANNs are data intensive tasks rather than computational ones since the computation tasks are simple with heavy memory access for the entire processing. Although both applications require data intensive processing, their behavioral models are different. The simulation of diffusion equations includes data transfer among PUs and the mapping of ANNs requires multiple memory indexing modes in each PU.

The rest of this paper is organized as follows. In Sect. 2, we describe the architecture and operation of the proposed processor. Section 3 shows the result of our performance evaluation. Section 4 provides the implementation result. Finally, we conclude in Sect. 5.
2. Processor Architecture

The proposed processor employs an SIMD architecture consisting of 16 processing units (PUs), a non-linear functional unit (NFU), and a control unit (CU), which are connected through two global data buses, one control bus, and a ring bus as shown in Fig. 1. The instruction program is stored in the embedded program memory, on the other hand, the data are distributed in embedded local memories (LMs) and external data memory. The global data bus and ring bus allow data broadcast and PU-to-PU data transfer. The CU generates the control signals for all PUs and allows address jump and branch functions. The NFU is a look-up table memory that realizes an arbitrary non-linear function. GRF (global register file) is used to store data from NFU. The data in GRF are to be broadcasted to PUs through the data bus or the ring bus.

Figure 2 shows the block diagram of a PU. Each PU consists of 16-bit fixed point numerical arithmetic units, a 16-bit 16-word register file, 16-bit 1.5 k-word LM, special purpose registers (CR, FR, and AR), and an address modifier (AM). In addition, a 16-bit logical arithmetic unit (LALU) is embedded for basic logical operations (AND, OR, XOR, and NOT) and two special purpose logical instructions (CONCATENATE and SHRINK). For MAC (multiply and accumulate) operation, the result of multiplier is bypassed to adder. The adder has the ability to perform the local memory addressing by adding the offset value stored in the RF0 register and the address field of WLD (or WST) instruction. The embedded LM is used to store weights, coefficients, image, and other data according to the applications. Followings are key features of the proposed processor.

2.1 Address Modifier (AM)

Particularly, each PU contains an AM which enables the proposed processor to have functionalities of both column-wise data fetch and row-wise data fetch. The importance to do so is that many linear algebra applications require series of matrix-by-vector and transposed matrix-by-vector multiplications. In ANNs, the matrix contains the synaptic weights and the vector does input values or error values. The matrix element accessing direction is dependent on the processing state.

Figure 3 shows an operational model of how an AM works on MLP (multi-layer perceptron) with backpropagation. Here, a row of the forward weight matrix is allocated to each PU. The first is feed-forward operation, in which the network computes the equation, $u_i = \sum_j s_j w_{ij}$. The second is error back-propagation that computes the equation, $e_j = \sum_i \delta_i w_{ij}$. From these two equations, the
weights distributed over LMs should be accessed in two different modes; the row-wise for the feed-forward and the column-wise for the error back-propagation. In the proposed processor, three mechanisms, ring, bus, and AM, are used for effective memory access for BP. For the process of feed-forward operation, the address is broadcast to all PUs simultaneously through bus as shown in Fig. 3 (a) since the weights are stored in local memories in row order. In error back-propagation phase, the AM calculates a new address using modular operation for column base memory access. Previous error values are shifted to next PU through ring register as shown in Fig. 3 (b). Therefore, the proposed architecture enables both row and column wise memory access without many overheads.

2.2 Multi-Chip Expansion

The expandability of the proposed processor is essential because most scientific computations require large sizes of parallel processing; Figure 4 shows the block diagram of multi-chip expansion. The multi-chip expansion through a register ring is used for increasing the network size. This is called as multi-chip ring shift operation mode which is decided by the flag attached to instructions. In this mode, the ring ready register is set to ‘1’ and the program is stalled. After all the ring ready registers in chips are set (or the signal, ext_shift_en, becomes ‘1’), the chip-to-chip ring shift operation is performed forming a larger ring across all the chips. This simplifies the chip-to-chip data transfer in multi-chips expansion. The contents of program memory of each chip are duplicated, and share the external data memory for multi-chip SIMD operation.

2.3 Instruction Set

The function of the proposed processor is programmed by means of 26 customized instructions for target applications. They include instructions for memory access, data transfers, arithmetic operations, and flow controls. Table 1 shows the instruction list including several special purpose instructions such as BR, WLD, SHRINK, CONCATENATE, etc.

BR is used for broadcasting data through ring or bus. The selection is made by the flag bit appended to BR instruction. WLD loads data from an LM of its neighbor PUs or its own PU to RF; at this time, the AM can be selected to operate on column-wise or row-wise memory access. SHRINK and CONCATENATE are special purpose instructions to increase the efficiency of bitwise filtering operations for the character recognition application. CONCATENAE creates a new word by combining two groups of bit from two input operands. One group of bits is taken from the first operand with the size of offset bits from MSB, while the other is taken from the second operand with the size of (16 bits - offset) bits from LSB. In SHRINK, the input operand is sequentially divided into several sub-blocks with the size of offset bits and the bit-wise operation is performed for all bits in each sub-block, and the results are stored in an output operand.

3. Verification

The functionality and the performance of the proposed processor are verified with the character recognition application based on ANNs including image processing and the simulation of diffusion equations for oil reservoir. We have programmed those applications and estimated the speed performance.

3.1 Character Recognition

Figure 5 shows the overall architecture of the proposed char-
character recognition system. Generally, the character recognition application is separated into three phases [16]. The first phase is the image pre-processing using translation, dilation, rotations, thinning, and so on to bring a character to a standardized form. The second phase is the feature extraction that corresponds to linear or non-linear filtering. The third phase is the classification based on features that are obtained in the second phase. If the recognition system requires learning or adaption, then additional learning or training stage is required.

3.1.1 Preprocessing and Feature Extraction

The pre-processing and the feature extraction consist of 4 stages; thinning, image filtering, connection, and shrinking. These operations are based on two dimensional morphological filtering [17].

The thinning skeletonizes an input image while preserving its original shape. After that, the skeletonized image is filtered with 12 two-dimensional morphological feature filters like direction, angle, crossing, and T-crossing filters. Each feature extraction filtering is performed in each PU and the filter weight is stored in LM. The input image is broadcasted through the data bus and the filter output is stored in LM. During the image filtering certain lines may be broken. These broken lines have to be reconnected by the connection process that is a morphological dilation. Then the object in the resulting image is shrunk down until only one point remains for each object. The number of renaming point is counted for each feature filter and it represents how many corresponding features are in the input image. These numbers are used as an input vector for the classifier that is realized through MLP with back-propagation learning.

3.1.2 MLP

MLPs are well-established multipurpose classifying algorithm, and they are frequently employed in recognition systems. On the proposed system, the MLP consists of three layers; input, output, and one hidden layer. Each layer consists of 16 nodes. To improve recognition performance, the input character sets are grouped into one of four sub-nets according to the number of strokes in the character.

Figure 6 shows the general structure of MLP with memory access mode on feed-forward and back-propagation stages. Table 2 shows the equations. Each PU is assigned for one neuron on a layer. Therefore, one PU holds two weight sets, one for the first layer and the other for second layer. The feed-forward path is processed with one input element at a time. The first input element $z_1$ is broadcasted through the data bus and all PUs compute the corresponding synaptic weight using $v_{ji}$ stored in each PU, and then the second input element $z_2$ is broadcasted through the data bus. The same operations are repeated for all input elements and the result of synaptic weight for every input is accumulated at AR in each PU. This is the process between the input layer and the hidden layer, which can be express as the equation,

$$net_j = \sum_{i=0}^{L-1} v_{ji}z_i.$$  

After that $net_j$ is moved to NFU through OR (output register) to calculate the output value $y_i = f_j(net_j)$ for the hidden layer. At this time, $y_i$ is also stored at global memory since it is going to be read again on back-propagation stage. The same sequence of computations for the second layer is repeated to calculate the $o_k$ in output neuron using the input $y_i$. This process...
can be expressed by the equations
\[ net_k = \sum_{i=0}^{k-1} w_{ki} y_j \]
and
\[ o_k = f_k (net_k). \]

In the back-propagation stage, the produced output \( o_k \)
is compared with the desired output \( d_k \) and an error value
\[ \delta_{ok} = (d_k - o_k) f'_k(\text{net}_k) = (d_k - o_k) o_k (1 - o_k) \]
is propagated backward to update weight values. The process is expressed
as following equations; \( \delta_{ok} = (d_k - o_k) f'_k(\text{net}_k) \) and \( w_{kj} = w_{kj} + \eta \delta_{ok} y_j \) between the output layer and the hidden layer;
\[ \delta_{yj} = \left( \sum_{k=0}^{k-1} \delta_{ok} w_{kj} \right) f'_k(\text{net}_k) \] and \( v_{ji} = v_{ji} + \eta \delta_{yj} \) between the hidden layer and the input layer. Finally, the weight is
updated using \( \delta_{yj} \).

These operations can be summarized as follows. First, the weight is expressed in the form of two dimensional
matrix and stored in local memory in row order. Second, the input
values are broadcasted to all PUs through the bus on the
feed-forward stage. Therefore, all PUs read weights at the
same memory location and execute MAC operation. Third,
on back-propagation stage the AM modifies the memory
address and the weights are read and calculated. And the desired
values are broadcasted through the ring. This allows the
proposed processor to operate on both row and column
mode memory access without overhead.

Another feature is that the calculation of non-linear function. The non-linear function requires complex compu-
tation or large look-up table. Implementation of such block
in each PU significantly increases the hardware complexity.
Therefore, only one NFU is implemented as a look-up ta-
ble. In this case, the computation of non-linear function will
become one of steady-state pressure distribution. Note that
Eq. (2) is equivalent to the original discrete reservoir equation
provided that the grid size along the x and y directions
are equal (i.e. \( \Delta x = \Delta y \)). Equation (1) can be solved iter-
avely with the proposed processor by defining:
\[ p_{i,j} = \alpha_{i,j}(p_{i-1,j} - p_{i,j}) - \alpha_{j-1,j}(p_{i,j} - p_{i-1,j}) + \beta_{i,j}(p_{i,j-1} - p_{i,j}) - \beta_{i,j+1,j}(p_{i,j} - p_{i,j+1,j}) + \chi_{i,j} \]
\[ p_{i,j}^* = p_{i,j} + \beta_{i,j} p_{i,j} \]
The definition for the lumped system parameters used in the
equation above and their relationship to the original reservoir
parameters are given in Eq. (4). Those symbols (\( \alpha, \beta, \) and \( \chi \)) are parameters of each cell obtained from geological
exploration.
\[ \alpha_{i,j} = \frac{1}{2 \Delta x^2} h_{i,j} k_{i,j} \]
\[ \chi_{i,j} = \frac{C \mu}{\Delta x \Delta y} q_{i,j} \]
\[ \beta_{i,j} = C_1 \mu \phi_{i,j} h_{i,j} \]

Simulation of a diffusion equation for oil reservoir is a data
intensive processing which is used to predict the future oil
production of an oil reservoir based on geological data of
the reservoir. In the petroleum industry, the demand for fast
simulation of dynamics in the reservoir is ever increasing.

The oil reservoir problem can simply be mapped into a
Resistor-Capacitor (RC) network for solving a system of
dynamic equations [18]. The discrete form of the parabolic
PDE describing pressure transient response during a well
test is given in Eq. (1). Here, \( p_{i,j} \) is the fluid pressure of the
cell located at \( (i, j) \).

\[
0 = \frac{1}{2 \Delta x^2} \left[ (h_{i,j} k_{i,j} + h_{i+1,j} k_{i+1,j})(p_{i+1,j} - p_{i,j}) + (h_{i-1,j} k_{i-1,j} + h_{i,j})(p_{i,j} - p_{i-1,j}) \right] \\
+ \frac{1}{2 \Delta y^2} \left[ (h_{i,j} k_{i,j} + h_{i,j+1} k_{i,j+1})(p_{i,j+1} - p_{i,j}) + (h_{i,j} k_{i,j} + h_{i,j})(p_{i,j} - p_{i,j-1}) \right] \\
- \left( h_{i,j} k_{i,j} \right)(p_{i,j} - p_{i,j-1})
\]
However, the simulation time of a large reservoir that is divided into millions of grid blocks due to the large number of elements in typical meshes. The problem grows very steeply as the grid size increases.

Figure 7 shows a part of program code for oil reservoir simulation. Most of operations consist of data read, addition, and multiplication. On the proposed processor, the whole grid is divided into several sub sections. Each PU stores geological data for each sub section on its LM. The boundary cell data on neighboring PU can be accessed through ring bus. This mechanism deals effectively with data-transfer intensive operations. Furthermore, multi-chip expansion mode easily provides the massive parallel processing as the mesh size grows.

4. Implementation Result

Figure 8 shows the physical layout of the prototype system board using the proposed processor architecture embodied in FPGA chip. Table 3 summarizes the FPGA implementation result and the specifications of the proposed processor. The operating clock is 15 MHz. The overall size is utilizing 29,923 logic elements equivalent to 120 million gate level.

The implemented recognition system is trained with 20 sets of 17 handwritten Korean alphabets for 1,770 iterations on incremental learning mode. Figure 9 shows that 4 MLPs successfully trained. It took 68 seconds for pre-processing, feature extraction, classification, and learning. In order to compare its processing time, the application was implemented by using C++ program running on 1.7 GHz Pentium IV personal computer with 512 MB DRAM, and its processing time was 19 seconds. The proposed processor showed no more than 3.5 times slower performance than PC-implementation, but nevertheless it run with relatively very slow operation clock of 15 MHz and small memory capacity of 50 KB embedded SRAM. Suppose the proposed processor is implemented as a chip using 0.18-micron process technology, it is expected to operate at 200 MHz clock speed, and then its computing power could be over 3 times faster than 1.7 GHz PC.

For diffusion equations, we estimate the computation speed according to the variation of mesh size. The following methods allow us to obtain the execution time in terms of CPU clock cycles. We use Pentium's RDTSC (Read Time Stamp Counter) [19] instruction to measure the execution time of the application implemented with C++ program on 1.7 GHz Pentium IV personal computer. The execution time was obtained by executing the code five times inside a loop, and then summed averaged execution time was selected. This was done to include all cache effects and to ensure the in-order execution of the RDTSC instruction, therefore, that execution time reported from the experiment represents the processor's best performance. In the proposed processor, the execution time information is obtained by calculating based on the processing time of one chip with 16 PUs. The

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>number of logic elements</td>
<td>29,923</td>
</tr>
<tr>
<td>clock frequency</td>
<td>15 MHz</td>
</tr>
<tr>
<td>embedded memory</td>
<td>1.5V</td>
</tr>
<tr>
<td>program memory</td>
<td>32-bit * 4K-word</td>
</tr>
<tr>
<td>register file</td>
<td>32-bit * 16-word</td>
</tr>
<tr>
<td>PC (program counter)</td>
<td>16-bit adder</td>
</tr>
<tr>
<td>decoding logic</td>
<td>4-bit adder</td>
</tr>
<tr>
<td>NPU memory</td>
<td>6-bit * 512-word</td>
</tr>
<tr>
<td>16-bit data bus</td>
<td>16-bit 16-bit ring chain</td>
</tr>
<tr>
<td>number of PUs/Chip</td>
<td>16</td>
</tr>
<tr>
<td>data path</td>
<td>16-bit fix point</td>
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<tr>
<td>local memory</td>
<td>16-bit * 1.0K word</td>
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<tr>
<td>arithmetic ALU</td>
<td>16-bit adder / subtractor</td>
</tr>
<tr>
<td>logical ALU</td>
<td>16-bit multiplier</td>
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<tr>
<td>logical ALU</td>
<td>16-bit boolean operators (AND, OR, XOR),</td>
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<tr>
<td>register file</td>
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<tr>
<td>special registers</td>
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<tr>
<td>Instruction set</td>
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<td>number of instructions</td>
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<td>opcode</td>
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</table>

![Fig. 8](image-url) System board with FPGA chip.

![Fig. 9](image-url) Convergence result from the independent chip.
execution time information is obtained by running the system board. The result shows that the execution time of the proposed processor outperforms PC implementation as the mesh size grows over 70 by 70 as shown in Fig. 10.

5. Conclusion

This paper proposed a high performance acceleration processor optimized for scientific computations such as diffusion equations and ANNs. Highly customized 26 instructions were devised to improve the performance and the programmability of the processor on the target applications. From the architectural point of view, the characteristic of the proposed processor is SIMD with 16 PUs and special hardware resources such as NFU, a ring, and buses. The proposed architecture is suitable for applications that require heavy memory access relatively low computational complexity. Furthermore, the AM in each PU enables the proposed processor to have the ability to operate on column wise and row wise memory access, which can be exploited by many linear algebra applications. Very simple multi-chip expansion is available for massively parallel processing. The prototype chip was implemented with FPGA. The functionality and performance of the proposed processor was verified with oil reservoir simulation and character recognition application. The former shows that the proposed processor outperforms 1.7 GHz Pentium IV PC as the mesh size grows over 70 by 70. The latter shows that the proposed processor has the possibility to achieve over 3 times better computation power than the PC, being implemented as a chip using 0.18-micron process technology.

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